# Standard Test Method for Non-Destructive Photoelastic Measurement of Edge and Surface Stresses in Annealed, Heat-Strengthened, and Fully Tempered Flat Glass ${ }^{1}$ 


#### Abstract

This standard is issued under the fixed designation C 1279; the number immediately following the designation indicates the year of original adoption or, in the case of revision, the year of last revision. A number in parentheses indicates the year of last reapproval. A superscript epsilon $(\epsilon)$ indicates an editorial change since the last revision or reapproval.


$\epsilon^{1}$ Note-Equation 11 was editorially revised in October 2001.

## 1. Scope

1.1 This test method covers the determination of edge stresses and surface stresses in annealed, heat-strengthened, and fully tempered flat glass products.
1.2 This test method is non-destructive.
1.3 This test method uses transmitted light and is, therefore, applicable to light-transmitting glasses.
1.4 The test method is not applicable to chemicallytempered glass.
1.5 Using the procedure described, surface stresses can be measured only on the "tin" side of float glass.
1.6 Surface-stress measuring instruments are designed for a specific range of surface index of refraction.
1.7 This standard does not purport to address all of the safety concerns, if any, associated with its use. It is the responsibility of the user of this standard to establish appropriate safety and health practices and determine the applicability of regulatory limitations prior to use.

## 2. Referenced Documents

2.1 ASTM Standards:

C 162 Terminology of Glass and Glass Products ${ }^{2}$
C 770 Test Method for Measurements of Glass StressOptical Coefficient ${ }^{2}$
C 1048 Specification for Heat-Treated Glass: Kind HS, Kind FT Coated and Uncoated Glass ${ }^{2}$
F 218 Test Method for Analyzing Stress in Glass
2.2 Other Documents:

Engineering Standards Manual ${ }^{3}$
"Surface and Edge Stress in Tempered Glass"4

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## 3. Terminology

3.1 Definitions:
3.1.1 analyzer-a polarizing element, typically positioned between the specimen being evaluated and the viewer.
3.1.2 polarizer-an optical assembly that transmits light vibrating in a single planar direction, typically positioned between a light source and the specimen being evaluated.
3.1.3 retardation compensator-an optical device, variants of which are used to quantify the optical retardation produced in transparent birefringent materials: typically positioned between the specimen being evaluated and the analyzer.
3.2 For definition of terms used in this test method, refer to Terminology C 162.

## 4. Summary of Test Methods

4.1 Two test methods are described in this standard:
4.1.1 Procedure A describes a test method for measuring surface stress using light propagating nearly parallel to the surface.
4.1.2 Procedure $B$ describes a test method for measuring edge-stress using light propagating in the direction perpendicular to the surface.
4.2 In both methods, the fundamental photoelastic concept is used. As a result of stresses, the material becomes optically anisotropic or birefringent. When polarized light propagates through such anisotropic materials, the differences in the speed of light rays vibrating along the maximum and minimum principal stress introduce a relative retardation between these rays. This relative retardation is proportional to the measured stresses, and can be accurately determined using compensators. For additional background see "Surface and Edge Stress in Tempered Glass" ${ }^{4}$.

## 5. Significance and Use

5.1 The strength and performance of heat-strengthened and fully-tempered glass is greatly affected by the surface and edge stress induced during the heat-treating process.
5.2 The edge and surface stress levels are specified in Specification C 1048, in the Engineering Standards Manual ${ }^{3}$ of GTA and in foreign specifications.
5.3 This test method offers a direct and convenient way to non-destructively determine the residual state of stress on the surface and at the edge of annealed and heat-treated glass.

## 6. Principles of Operation

### 6.1 Procedure A: Measuring Surface Stress:

6.1.1 Measurement of surface stresses requires an optical apparatus that permits the injection of polarized light rays propagating in a thin layer adjacent to the surface (see Note 1). A prism is usually used for this purpose. The rays emerge at critical angle $i_{c}$. The photoelastic retardation due to the surface stresses, (see Fig. 1), is measured using a wedge-compensator.
6.1.2 The incident light beam should be arriving at the critical angle $i_{c}$ and polarized at $45^{\circ}$ to the entrance of the prism edge. A quartz wedge-compensator, $W_{c}$, placed in the path of emerging light adds a retardation, $R_{c}$, to the retardation $R_{s}$ induced by stresses in the surface of the specimen. The analyzer, $A$, placed between the eyepiece, $E$, and the wedgecompensator, $W_{c}$, generates a visible set of fringes or lines of constant retardation $R$ where

$$
\begin{equation*}
R=R_{s}+R_{c} \tag{1}
\end{equation*}
$$

Since the specimen-induced retardation is proportional to the surface stress, $S$, and the path, $t$, we have:

$$
\begin{equation*}
R_{s}=C \cdot S \cdot t=C \cdot S \cdot a x \tag{2}
\end{equation*}
$$

where:
$R=$ is the relative retardation,
$C=$ stress-optical constant (see Note 2),
$S=$ surface stress in the direction perpendicular to the path, t
$t=$ path of light traveling between the entrance and exit points 1, 2 (Fig. 1),
$a=$ Geometrical factor, (depending upon the prism design) $a=t / x$. This constant is determined by the manufacturer.
6.1.3 The compensator adds its own retardation. It is linearly variable along its length $y$ and is calculated as


$$
\begin{equation*}
R_{c}=b \cdot y \tag{3}
\end{equation*}
$$

Where $b$ is a constant, determined by the manufacturer of the compensator. The observer sees in the compensator plane a total retardation $R$.

$$
\begin{equation*}
R=R_{s}+R_{c}=a \cdot C \cdot S \cdot x+b \cdot y \tag{4}
\end{equation*}
$$

6.1.4 The fringes (lines of $R=$ Constant) are, therefore, tilted lines. (See Fig. 2). The angle $\theta$ is the tilt of these fringes relative to a plane containing the light path of Figs. 1 and 2. The measured stress is proportional to the tangent of the tilt angle $\theta$, measured using a goniometer, and to an instrument calibration constant, K MPa (psi), determined by the manufacturer.

$$
\begin{gather*}
\tan \theta=\frac{a \cdot C \cdot S}{b} \text { and }  \tag{5}\\
\text { Stress }=\frac{b}{C a} \cdot \tan \theta=K \cdot \tan \theta
\end{gather*}
$$

In the actual procedure (see 9.1 below) the operator measures the tilt angle $\theta$ of the observed set of fringes.

Note 1—The surface-stress measuring apparatus described in this section is manufactured by Strainoptic Technologies, Inc. in North Wales, Pennsylvania.

Note 2-The stress constant of float glass is typically 2.55 to 2.65 Brewsters. Calibration can be performed using one of the test methods described in Test Methods C 770.

### 6.2 Procedure B: Measuring Edge Stress:

6.2.1 Measurement of edge stress is accomplished using a polarimeter equipped with a wedge-compensator, as shown schematically in Fig. 3.
6.2.2 The angle between the polarizer and the edge of the specimen must be $45^{\circ}$ (see Fig. 3a), and the analyzer must be perpendicular to the polarizer. The overall magnification should be at least $20 \times$ to permit clear visibility of the reticle, and of photoelastic fringes near the edge. The reticle placed adjacent to the specimen must have graduations of 0.1 mm ( 0.004 in .) or smaller. The resolution of the compensator should be at least 5 nm , and the compensator should be calibrated by the manufacturer at 565 nm wavelength with results of calibration expressed in $\mathrm{nm} / \mathrm{div}$.


FIG. 1 Apparatus For Measuring Surface Stress

Rotate protractor to align crosshair paralle with observed fringes

Read angle $\theta$ and use Equation 4 to convert angle $\theta$ to stress


FIG. 2 Fringes Observed in the Plane of the Compensator


FIG. 3 Schematic of the Instrument for Measuring Edge Stress


FIG. 4 Orientation of the Instrument for Measuring Surface Stress
6.2.3 The compensator used could be of linear wedge type (Babinet) or uniform-field type (Babinet-Soleil). The linearwedge type requires a reticle placed adjacent to the compensator wedge and a linear-motion scale, or lead screw, locating the wedge position with reference to the reticle.


FIG. 5 Depth Measurement of Beveled Region
6.2.4 The uniform field does not require a reticle, and must be equipped with a lead screw measuring the relative motion of its wedges.

## 7. Sampling

7.1 Procedure A: Measuring Surface Stress-The number of points to be measured are determined by the product specification.
7.2 Procedure B: Measuring Edge Stress- Readings must be obtained at the mid-span point of every edge.

## 8. Conditioning

8.1 In order to avoid thermal stresses, the specimen should be allowed to reach ambient temperature throughout its entire mass prior to testing.

## 9. Procedure

9.1 Procedure A-Measuring Surface Stress:
9.1.1 Clean the surface of any trace of oil or other chemical deposits.
9.1.2 Place a few drops of index liquid on the tin side surface of the specimen at the point of interest. The index of refraction of the liquid should be higher than the index of the examined glass and lower or equal to the index of the prism.
9.1.3 Perform the adjustments of the optical path in accordance with manufacturer's specifications to obtain a clear image of an equally-spaced set of fringes in the compensator plane.
9.1.4 Using the goniometer, measure the angle $\theta$ (in degrees) of these fringes to the plane of symmetry (see Fig. 2).
9.1.5 In all instances where the surface stress is uniform (independent of direction), measure the angle $\theta$, orienting the instrument's plane of symmetry to measure stress parallel to the nearest edge.
9.1.5.1 In those instances where the direction of maximum and minimum stress is uncertain (as a result of irregular geometry, proximity of edges, or non-uniformity of heattreating process), orient the instrument along direction $\alpha_{1}, \alpha_{2}$, $\alpha_{3}$, and measure the fringe pattern angle $\theta_{1}, \theta_{2}, \theta_{3}$, in degrees, for each direction. Select $\alpha_{1}, \alpha_{2}, \alpha_{3}$ as follows:
$\alpha_{1}$ parallel to the nearest edge,
$\alpha_{2} 45^{\circ}$ to the nearest edge, and
$\alpha_{3}$ perpendicular to the nearest edge. (See Fig. 4)
9.2 Procedure B—Measuring Edge Stress:
9.2.1 Place the instrument in position, with a measuring reticle placed adjacent to instrument, and in close contact with the edge of glass.


FIG. 6 a) Fringes Observed Using Wedge Compensator (Babinet), b) Fringes Observed Using Double Wedge Compensator (Babinet-Soleil)
9.2.2 Using the reticle graduation, measure the depth, $d$, in mm (in.), of the seamed or beveled region, which is nontransmitting. If the depth of the beveled region, $d$ (see Fig. 5), is less than 0.25 mm ( 0.010 in .), use visual extrapolation of the observed fringe pattern (see 9.2.3). When the depth is equal to or greater than $0.25 \mathrm{~mm}(0.010 \mathrm{in}$.), use the extrapolation equation (see 9.2.5).
9.2.3 Measurement Using Visual Extrapolation-Observe the pattern of photoelastic fringes near the edge of the specimen (see Fig. 6a and Fig. 6b). Adjust the wedge (or double wedge) until the black fringe arrives to the edge (double wedge, Fig. 6b), or crosses the edge at the crosshair (single wedge, Fig. 6a).
9.2.4 Obtain a reading $\left(R_{e}\right)$ using a single or double wedge, at the center of each edge of the glass.
9.2.5 Measurement Using an Extrapolation Equation-In case the seamed edge makes the reading at the edge difficult [ $d$ $>0.25 \mathrm{~mm}(0.01 \mathrm{in})$.$] , measurement of retardation R(\mathrm{~nm})$ at two points, $x_{1}$ and $x_{2}$ (Fig. 6b), of the reticle scale must be made. These points are to be selected per Table 1. The retardations $R_{l}$ and $R_{2}(\mathrm{~nm})$ are retardation values measured using the compensator scale at the points $x_{1}$ and $x_{2}$. The edge retardation $R_{e}(\mathrm{~nm})$ is obtained from the equation:

$$
\begin{equation*}
R_{e}=3.8 \cdot R_{1}-2.8 \cdot R_{2} \tag{6}
\end{equation*}
$$

9.2.6 Using a micrometer, measure the thickness of the specimen at the location where the stress is measured.

## 10. Calculation and Interpretation

10.1 Procedure A: Measuring Surface Stress-When the measured angle is obtained using procedure 9.1.5, calculate the surface stress, $S$, using:

$$
\begin{equation*}
S=K \tan \theta \tag{7}
\end{equation*}
$$

where $K$ is the instrument calibration constant determined by the manufacturer, in MPa (psi).
10.1.1 In those instances where the surface stress is directional, assess the state of stress by comparing the reading $S$ in three directions $\alpha_{1}, \alpha_{2}, \alpha_{3}$. If all three directions yield the same measured angles $\theta_{1}, \theta_{2}, \theta_{3}$ within $1^{\circ}$, calculate the average angle, then obtain the surface stress from Eq 8 and Eq 9 .

$$
\begin{equation*}
\theta_{\text {average }}=\frac{\theta_{1}+\theta_{2}+\theta_{3}}{3} \tag{8}
\end{equation*}
$$

$$
\begin{equation*}
S=K \cdot \tan \theta_{\text {average }} \tag{9}
\end{equation*}
$$

If the measured angles $\theta_{1}, \theta_{2}$, and $\theta_{3}$ differ by more than $1^{\circ}$, then using Eq 7, obtain the three stresses $S_{1}, S_{2}$, and $S_{3}$ in directions $\alpha_{1}, \alpha_{2}$, and $\alpha_{3}$, and then calculate the principal stresses $\mathrm{S}_{\text {max }}$, and $\mathrm{S}_{\text {min }}$, from Eq 10 and Eq 11.

$$
\begin{align*}
S_{\max } & =\frac{S_{1}+S_{3}}{2}+\frac{\sqrt{2}}{2} \sqrt{\left(S_{1}-S_{2}\right)^{2}+\left(S_{2}-S_{3}\right)^{2}}  \tag{10}\\
S_{\min } & =\frac{S_{1}+S_{3}}{2}-\frac{\sqrt{2}}{2} \sqrt{\left(S_{1}-S_{2}\right)^{2}+\left(S_{2}-S_{3}\right)^{2}} \tag{11}
\end{align*}
$$

10.2 Procedure B: Measuring Edge Stress- From the measured retardation $R_{e}$ calculate the edge stress (in psi):

$$
\begin{equation*}
S_{e}=\frac{R_{e} \cdot b}{t C_{B}} \tag{12}
\end{equation*}
$$

TABLE 1 Location of Points $x_{1}$ and $x_{2}$

| Thickness of Glass |  |  |  |
| :---: | :---: | :---: | :---: |
|  | $1 / 8$ to $3 / 16$ inch ( 3 to 5 mm ) | $\begin{aligned} & 1 / 4 \text { to } 3 / 8 \mathrm{inch} \\ & (6 \text { to } 10 \mathrm{~mm}) \\ & \hline \end{aligned}$ | $\begin{gathered} 1 / 2 \text { to } 1 \mathrm{inch} \\ (12 \text { to } 24.5 \mathrm{~mm}) \\ \hline \end{gathered}$ |
| $\mathrm{x}_{1}$ | 0.6 or 0.8 mm | 1.0 mm | 2.0 mm |
| $\mathrm{x}_{2}$ | 1.0 or 1.3 mm | 1.6 mm | 3.0 mm |

where:
$R_{e}=$ the compensator reading ( nm ),
$t=$ the thickness of the glass sample (mm, in.),
$C_{B}=$ stress-optical constant, Brewsters (1 Brwstr. $=10^{-12}$ ) /Pa or nm/psi•n.,
$S_{e}=$ stress MPa (psi), and
$b=$ compensator constant, determined by manufacturer.

## 11. Report

11.1 At a minimum, the report must contain:
11.1.1 Date of specimen manufacture
11.1.2 Identification of specimen (material)
11.1.3 Selected procedure
11.1.4 Glass thickness
11.1.5 For surface measurement:
11.1.5.1 Location(s) of measurement(s)
11.1.5.2 Direction of measurement(s)
11.1.5.3 Values of $\theta_{1}, \theta_{2}, \theta_{3}$ at each location and the calculated stress
11.1.6 For edge measurements:
11.1.6.1 Location of measurement(s)
11.1.6.2 Chamfer size
11.1.6.3 Thickness of specimen at point of measurement
11.1.6.4 Extrapolation method used- visual (9.2.3) or calculated (9.2.5)
11.1.6.5 Average edge stress

## 12. Precision and Bias

12.1 An interlaboratory round robin testing was conducted in accordance with Practice E 691 to establish the precision and bias of surface stress measurements. Table 2 summarizes the result of this study. In this test, seven laboratories measured surface stress on six samples using Procedure A. Each test result was an average of 3 replicates. The samples used exhibited a broad range of stress levels. A thorough analysis of raw data and intermediate calculation was filed in a Research Report format with ASTM.
12.2 The results shown in Table 2 summarize the statistical analysis using data collected at the same location (point "A") of all samples, and lists both the measured fringe angle ( in degrees) and the calculated stress. Test data were collected at 5 points of each sample. A considerable variation of surface
stress was measured within each sample, yielding a substantial data scatter. The variability of stress in each sample was substantially higher than the reproducibility of measurements at an individual point
12.3 In Table 2, the repeatability standard deviation $\mathrm{S}_{\mathrm{r}}$ expresses an average of "within laboratory" reproducibility and the standard deviation $S_{x}$ expresses interlaboratory deviation. The stress was calculated from the measured angle using Eq. (4). There is no assurance that all instruments used in the round robin were calibrated to verify their conformance to factory specification.
12.4 Bias-The calibration and instrument constant K used to convert measured fringe angle $\theta$ to stress is affected by the material stress-optical constant C and the index of refraction of the measured sample. Disregarding these changes will result in a systematic error that can be only eliminated when the calibration of the instrument is performed on the same batch of material as the measured sample.

## 13. Keywords

13.1 annealed glass; heat-strengthened glass; polariscopic examination; stress measurement; tempered glass

TABLE 2 Result of Statistical Data Analysis
(Measuring Stresses in direction X and Y at a point "A" in all samples.)

| Sample \# | 14 |  | 13 |  | 17 |  | 16 |  | 18 |  | 15 |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Point A | Stress direction |  | Stress direction |  | Stress direction |  | Stress direction |  | Stress direction |  | Stress direction |  |
|  | x | y | x | y | x | y | x | y | x | y | x | y |
| Average measured angle ${ }^{\text {A }}$ | 23.6 | 29.6 | 53.4 | 54.1 | 55.4 | 55.4 | 61.5 | 64 | 68.4 | 68.4 | 70.6 | 71.9 |
| Average stress, $\mathrm{psi}^{\text {A }}$ | 2657 | 3454 | 8188 | 8401 | 8815 | 8815 | 11200 | 12468 | 15359 | 15359 | 17268 | 18605 |
| Standard Deviation of Cell Averages, (eq. 5 of E691) Sx ${ }^{A}$ | 2.04 |  | 1.7 |  | 1.82 |  | 2.01 |  | 1.63 |  | 1.98 |  |
| Repeatability Std Dev. (eq 6 of E 691 ) $\mathrm{Sr}^{A}$ | 0.49 |  | 0.48 |  | 0.41 |  | 0.61 |  | 0.33 |  | 0.46 |  |
| Standard deviation, psi | 258 |  | 507 |  | 598 |  | 936 |  | 1274 |  | 1901 |  |

${ }^{A}$ Fringe angle in degrees.

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